

## Nuclear demagnetization →

Because nuclear magnetic moments are weak, nuclear magnetic interactions are much weaker than similar electronic interactions. We expect to reach a temp. 100 times lower with a nuclear paramagnet than with an electron paramagnet.

The initial temperature  $T_1$  of the nuclear stage in a nuclear spin cooling experiment must be lower than in an electron spin-cooling experiment. If we start at  $B = 50 \text{ kG}$  and  $T_1 = 0.01 \text{ K}$ , then

$$\mu_B / k_B T_1 \approx 0.5$$

and the entropy decrease

on magnetization is over 10% of the maximum spin entropy. This is sufficient to overwhelm the lattice and from

$$T_2 = T_1 (B_0/B)$$

where  $B$  is the initial field.

now we estimate a final temp.  $T_2 = 10^{-7}$  K.  
 The first nuclear cooling experiment carried out on Cu nuclei in the metal, starting from a first stage at about 0.02 K as attained by electronic cooling. The lowest temp. reached was  $1.2 \times 10^{-6}$  K.

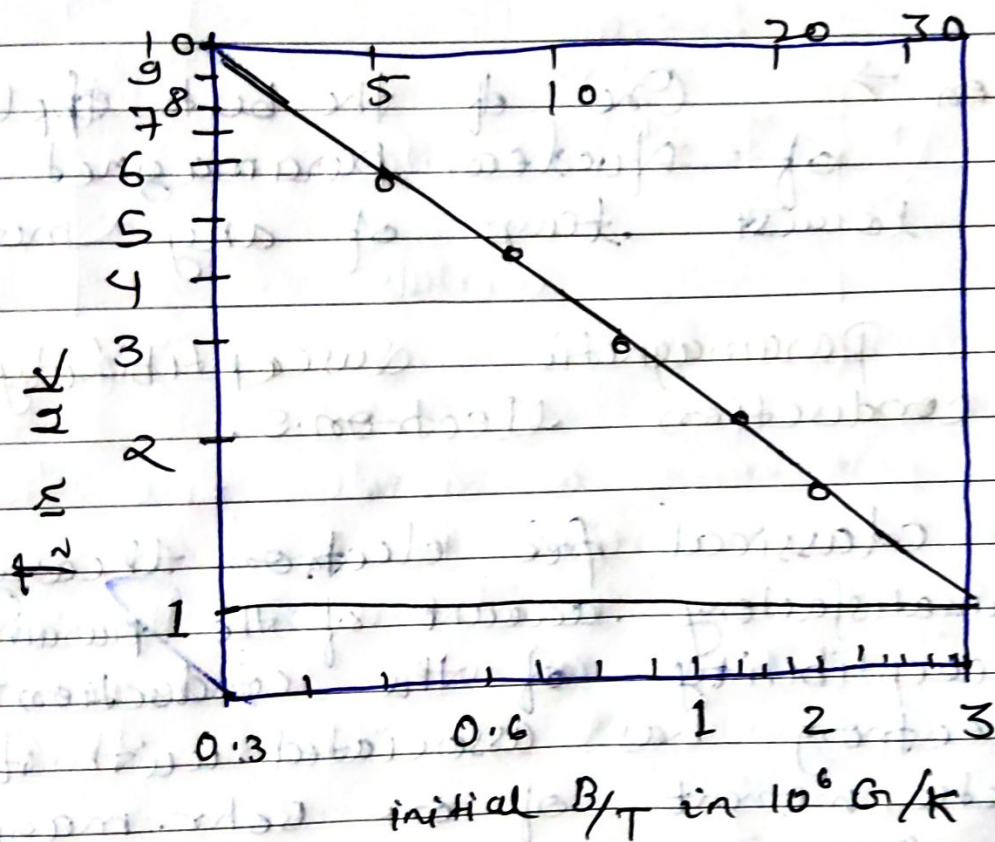


fig. Nuclear demagnetization of Cu nuclei in the metal, starting from 0.012 K and various fields.

The results in above fig fit a line of the form of  $T_2 = T_1 (B_\Delta / B)$  as  $T_2 = T_1 (3.1 / B)$  with  $B$  in gauss, so that  $B_\Delta = 3.1$  Gauss. This is the effective interaction

field of magnetic moments of the Cu nuclei.

The motivation for using nuclei in a metal is that conduction electrons help ensure rapid thermal contact of lattice and nuclei at the temperature of the first stage.

Application  $\rightarrow$  One of the best applications of Nuclear Paramagnet is to obtain lowest temp of any metal.

Question (a) Paramagnetic susceptibility of conduction electrons.

Answer  $\rightarrow$  Classical free electron theory gives an unsatisfactory account of the paramagnetic susceptibility of the conduction electrons. An electron has associated with it a magnetic moment of one Bohr magneton,  $\mu_B$ . One might expect that the conduction electrons would make a Curie-type paramagnetic contribution

$$\frac{M}{B} \cong \frac{N J(J+1) g^2 \mu_B^2}{3k_B T} = \frac{N \mu_B^2}{3k_B T} = \frac{C}{T}$$

of the metal:  $M = N \mu_B^2 / k_B T$ .

Instead it is observed that the magnetization of most normal non-ferromagnetic metals is independent of temperature.

Pauli showed that the application of Fermi-Dirac distribution would correct the theory as required.

Most conduction electrons in a metal, however, have no possibility of turning over when a field is applied, because most orbitals in the Fermi sea with parallel spin array are already occupied. Only the electrons within a range  $k_B T$  of the top of the Fermi distribution have a chance to turn over in the field; thus only the fraction  $T/T_F$  of the total number of electrons contribute to the susceptibility.

Hence,

$$M \approx \frac{N \mu^2 B}{k_B T} \cdot \frac{T}{T_F} = \frac{N \mu^2}{k_B T_F} B$$

which is independent of temperature and of the observed order of magnitude.

We now calculate the expression for the paramagnetic susceptibility of free electron gas at  $T \ll T_F$ .

We follow the method of calculation suggested by below fig.

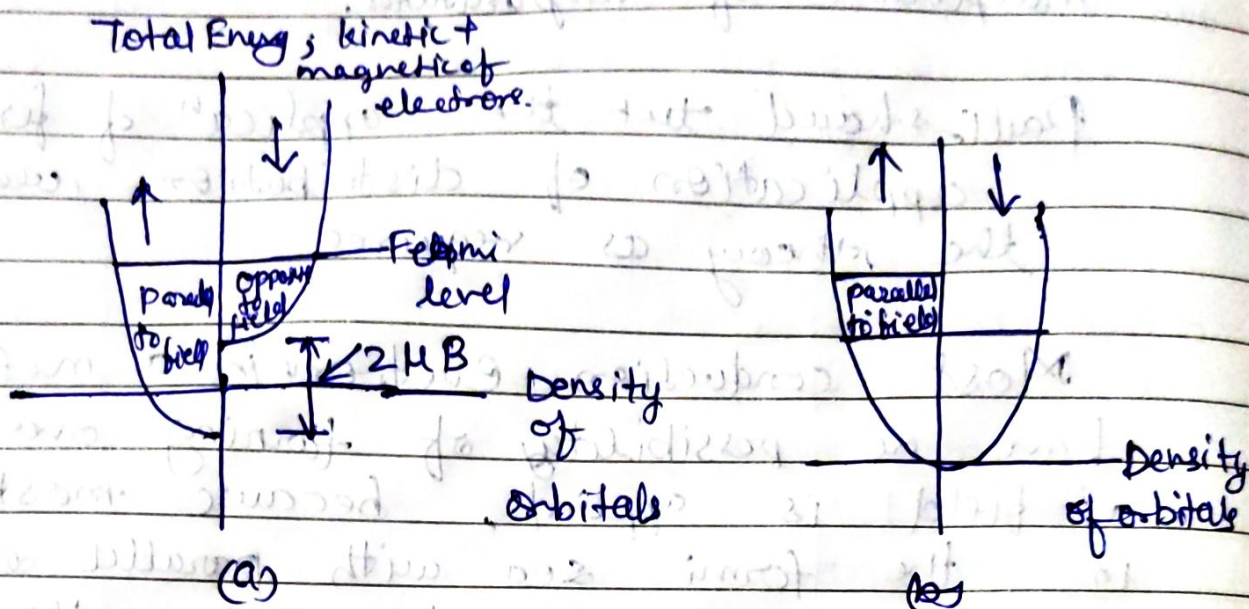


Fig → Pauli paramagnet at absolute zero the orbitals in the shaded region in (b) are occupied. The number of electrons in the "up" and "down" will adjust to make the energies equal at the Fermi level.

(b) we show the excess of moment up electrons in the magnetic field.

The concentration of electrons with magnetic moments parallel to the magnetic field is

$$N_{\uparrow} = \frac{1}{2} \int_{-\mu B}^{\epsilon_F} d\epsilon D(\epsilon + \mu B) \approx \frac{1}{2} \int_0^{\epsilon_F} d\epsilon D(\epsilon) + \frac{1}{2} \mu B D(\epsilon_F)$$

written for absolute zero. Here  $\frac{1}{2} D(\epsilon + \mu_B)$  is the density of orbitals of one spin orientation, with allowance for the downward shift of energy by  $-\mu_B$ . The approximation is written for  $k_B T \ll \epsilon_F$ .

The concentration of electrons with magnetic moments anti parallel to the magnetic field is

$$N_- = \frac{1}{2} \int_{\mu_B}^{\epsilon_F} d\epsilon D(\epsilon - \mu_B) = \frac{1}{2} \int_0^{\epsilon_F} d\epsilon D(\epsilon) - \frac{1}{2} \mu_B D(\epsilon_F)$$

The magnetization is given by  $M = \mu (N_+ - N_-)$ , so that

$$M = \mu^2 D(\epsilon_F) \cdot B = \frac{3N\mu^2}{2k_B T} \cdot B \quad (2)$$

with  $D(\epsilon) = \frac{3N}{2\epsilon_F} = \frac{3N}{2k_B T_F}$ .

Above eqn (2) gives the Pauli spin magnetization of conduction electrons.

Landau has shown that for free electrons wave function are modified. This causes a diamagnetic moment equal to  $-\frac{1}{3}$  of the parallel magnetic moment. Thus the total magnetic moment magnetization of a free electron gas is

$$M = \frac{N\mu^2}{k_B T} B$$